Fast Boundary Flow Prediction using Optimal Autoregressive Moving Average with Exogenous Inputs (ARMAX) Predictor

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Connected Corridors program by Berkeley PATH and Caltrans:

- Build decision support system for live TMC operations
- Short-term traffic prediction by cell-transmission model
- Requires short-term prediction of network boundary inflows



Empirical Loop Traffic Data



This paper: fast and reliable boundary flow predictor

- Based on months of historical data
- Combine historical average flow and recent flow
- Works in both regular and irregular conditions

Phenomena:

- Traffic repeats daily and weekly
- Small deviations every day

Overview of Methodology

Calibration:

Forecast:

- Data: Months of *historical flow data* based on California PeMS sensors

- Algorithm: *Cluster historical data* by day of the week and calculate centroid by median



Live Cluster Matching:

- Data: Live flow data from midnight to

Details

Idea:

Traffic flow = historical average + structural deviation of today + error

Autoregressive Moving Average with Exogenous Input model (ARMAX): Based on idea: $y^{\text{pred}}(k+1) = b_{-1}u(k+1) + b_0u(k) + b_1u(k-1) + ...$ $+ a_0y(k) + a_1y(k-1) + ...$ $+ c_0w(k) + c_1w(k-1) + ...$ y^{pred} : prediction; y: todays data; u: centroid; w: estimation residual; k: time step; a_i , b_i , c_i : ARMAX parameters Parameter estimation of a_i , b_i , c_i : live in every time step by least

squares

now

- Algorithm: *Determine todays centroid* based on day of the week (trivial)

- Algorithm: *Combine live data with*

todays centroid by applying ARMAX model

Features:

- ARMAX model reacts to structural deviations, e.g. caused by special events such as NFL Super Bowl game

- Prediction is fast, due to small amount of data

- Using median in calibration step is reliable w.r.t. outliers, e.g. caused by unusual traffic or sensor failures

- Calibration offline, which is slow due to large amount of data

Results: One-hour Prediction of Traffic Flow at a Network Boundary

y(k)

u(k)

 $v^{p}(k+1|k)$

 $y^{p}(k+2 \mid k)$

 $y^{p}(k+3 | k)$

 $y^{p}(k+4 | k)$

Day with irregular traffic pattern: Super Bowl Day

Day with regular traffic pattern: a working day







Mean Absolute Error of prediction by ARMAX: 501 veh/h Mean Absolute Error of prediction by historical average only: 703 veh/h Mean Absolute Error of prediction by ARMAX: 153 veh/h Mean Absolute Error of prediction by historical average only: 160 veh/h

